

Answer all the following questions: measures ILOs (a1,a2,a3,b1,b2,b3,c1,c2,c3)

Question No.1 (40 marks)

(Marks)

a-Draw the shear force and bending moment diagrams for the beam shown in Fig.(1-a)).(20)

b-Determine the moment of inertia of the section area shown in Fig. (1-b) with respect to the x-axis and y-axis. (10)

c-An anvil consisting of a rectangular prism and two circular cones is shown in Fig.1- c . Determine the mass moment of inertia with respect to x-axis, y-axis and z-axis. (10)

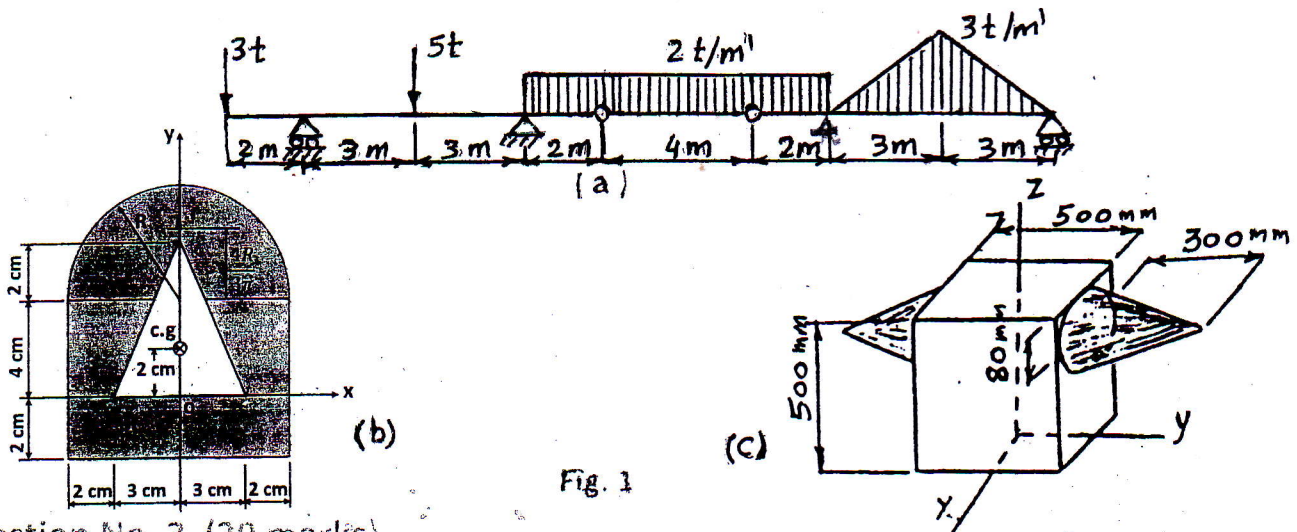


Fig. 1

Question No. 2 (20 marks)

A satellite is describing an elliptical orbit of eccentricity $e = 1/5$ around the earth with minimum distance from the earth center $r_0 = 10$ Mm as shown in Fig.2. Take the mass of the earth $m_e = 5.976 \times 10^{24}$ kg and the universal gravitational constant $G = 66.73 \times 10^{-12}$ m³/kg.sec², calculate :-

- a-The maximum and minimum velocities of the satellite v_0 and v_1 ,
- b-The periodic time τ ,
- c-if auxiliary rockets are fired, when the satellite is at point A_0 , to increase its velocity to escape velocity v_e , find the work done by the auxiliary rockets.The satellite mass 5 kg.

Question No.3 (15 marks)

Two spheres A and B each have a mass of 10 kg and the initial velocities shown in Fig.3 just before they collide . If the coefficient of restitution $e = 0.6$, determine their velocities just after the impact.



Question No. 4 (15 marks)

The pump shown in Fig.4 draws air with a rate of 6 kg/sec through the tube A of diameter D with a velocity v and discharges it at outlet velocity u through two tubes B of diameter d . If $v = 10$ m/s, $D = 0.8$ m, $d = 0.2$ m, $\alpha = 45^\circ$, determine :-

- The outlet velocity u , and
- The force F_x required supporting the pump.

Question No. 5 (15 marks)

Link AOB shown in Fig.5 rotates about the bearing O. A piston C is connected through a link BC which at the instant shown is vertical. Angle AOB is 120° where OA is horizontal. The point A has an upward velocity of 3 m/s and an upward acceleration of 1.5 m/s². Determine the linear velocity and acceleration of the piston C.

Question No. 6 (15 marks)

In Fig.6, a disk of radius $R = 50$ cm rotates about its axis oz with constant angular velocity $\omega_1 = 40$ rad/s. Simultaneously, it is embedded in a frame which rotates about the vertical axis oZ with a constant angular velocity $\omega_2 = 10$ rad/s. Determine :-

- The resultant angular velocity and angular acceleration of the disk,
- At the instant when the axis oz coincides with the axis oY , determine the linear velocity and acceleration of the point A on the disk, and
- The generated gyroscopic moment M_G if the moment of inertia of the disk about the axis oz is $I_z = 120$ kg·cm².

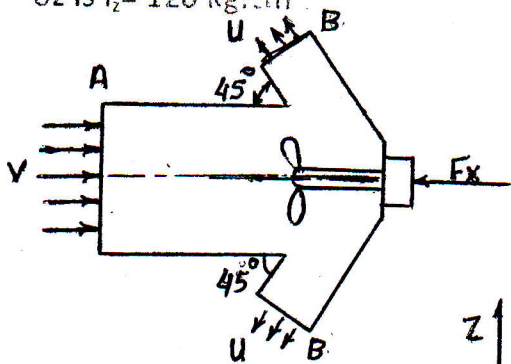


Fig 4

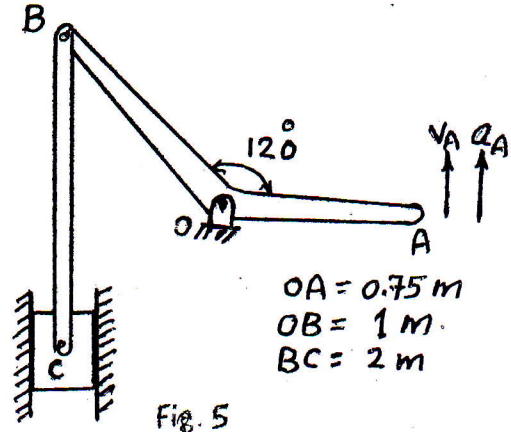


Fig. 5

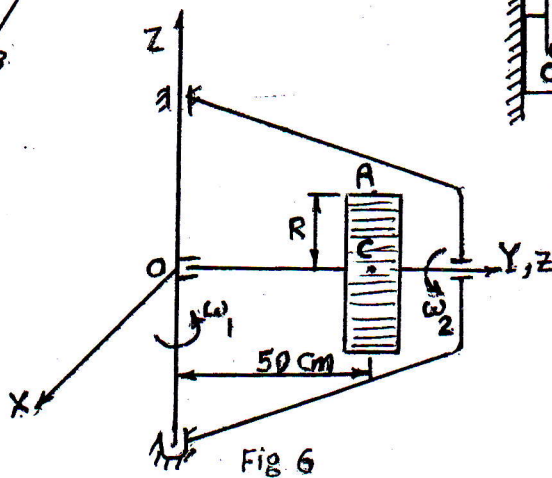


Fig 6

GOOD LUCK

With our best wishes

This exam measures the following (10s)

| Question Number | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|-----------------|----------------------------------|---------------------|---|---|---|---|---|---|---|---------------------|
| Skills | | | | | | | | | | |
| | Knowledge & Understanding Skills | Intellectual Skills | | | | | | | | Professional Skills |